$\tilde{A}_I, \tilde{S}_B$